



ENGINEERING STUDIES ATAR COURSE

DATA BOOK

2023

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Base International System (SI) units

Quantities	SI units		
Quantities	Names	Symbols	
Length	metre	m	
Mass	kilogram	kg	
Time	second	S	

Selected derived SI units

Derived quanties	Names	Symbols
Energy, work, quantity of heat	joule	J
Power	watt	W
Area	square metre	m ²
Volume (gas)	cubic metre	m³
Speed, velocity	metre per second	m s ⁻¹
Mass density	kilogram per cubic metre	kg m⁻³

Other units

Derived quanties	Names	Symbols
Temperature (Celsius)	degrees Celsius	°C
Volume (liquid)	litre	L

SI prefixes

Prefixes	Abbreviations	Multipliers		
Tera	Т	1012	= 1 000 000 000 000	
Giga	G	10 ⁹	= 1 000 000 000	
Mega	M	10 ⁶	= 1000 000	
Kilo	k	10 ³	= 1000	
		10 ⁰	= 1	
Milli	m	10-3	= 0.001	
Micro	μ	10-6	= 0.000 001	
Nano	n	10 ⁻⁹	= 0.000 000 001	
Pico	р	10 ⁻¹²	= 0.000 000 000 001	

Common constant

Item	Symbol	Value	
Pi	π	3.14159	

General formulae

Right triangular plane figures	Formulae
Pythagoras (side lengths)	$h^2 = o^2 + a^2$
	$\cos\theta = \frac{a}{h}$
Angular relationships	$\sin\theta = \frac{o}{h}$
	$\tan \theta = \frac{o}{a}$
Circles, cylinder and sphere figures	Formulae
Circumference $[C]$ of a circle	$C = \pi d$
Area [A] of a circle	$A = \pi r^2$
Surface area $[A]$ of open-ended cylinder	$A = \pi dh$
Surface area $[A]$ of a sphere	$A = 4\pi r^2$
Volume $[V]$ of a cylinder	$V = \pi r^2 h$
Volume $[V]$ of a sphere	$V = \frac{4}{3} \pi r^3$
Density, energy and efficiency	Formulae
Density $[ho]$	$ \rho = \frac{m}{V} $
Energy [E]	E = Pt
Efficiency [η] %	$\eta\% = \frac{output}{input} \times 100$

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Materials properties (at room temperature)

Materials	Density kg m ⁻³	Elastic (Young's) modulus kN mm ⁻²	Ultimate tensile * strength N mm ⁻²	Yield stress N mm ⁻²	Electrical conductivity Ω ⁻¹ m ⁻¹ × 10 ⁶	Thermal conductivity W m ⁻¹ K ⁻¹
Structural steel	7850	200	470	250	13.00	46
Stainless steel	7600	200	860	502	1.35	16
Cast iron	7200	120	180		10.30	80
Wrought iron	7750	200			10.30	80
Aluminium	2710	70	150	95	37.70	237
Brass	8740	90	190	50	16.70	109
Copper	8930	112	210	70	59.50	401
Zinc	7130	108	200	13.80	16.80	116
Solder	9280	23.7	37	_	7.28	43.60
Concrete	2400	30	40 (compressive)			0.80
Timber (parallel to grain)		12	105			0.16
Polypropylene	1240	4	19.7 – 80	50		0.13
Polycarbonate	1200	2.30	70			0.19
ABS plastics		2.30	40	48.30		2.34
Nylon	1160	2 – 4	75	45		
Acrylic	1190	3.20	70	73.70		0.19
	ı	T		I	I	
Glass	2500	69		3600		1.05
Diamond	3520	1000		50 000		2320
Gold	19 320	82	220	40	44.60	318
Ice	931	9.17(@-5°C)		85		2.25(@-5°C)
Pure water	1000	J.17(W-J C)		0.5		2.20(@-0 0)
Sea water	1022					
Joa Water	1022					
Petrol	740					0.15
Crude oil	800					0.15

^{*} Unless noted as compressive strength.

Materials formulae

Parameters	Formulae
Stress [σ]	$\sigma = \frac{F}{A}$
Strain [ε]	$\varepsilon = \frac{\Delta L}{L}$
Young's modulus $[E]$ (elastic modulus)	$E = \frac{\sigma}{\varepsilon}$
Young's modulus $[E]$ expanded formula	$E = \frac{FL}{A\Delta L}$
Factor of Safety [FS]	$FS = rac{\sigma_{UTS}}{\sigma_{safeworking}}$

Statics formulae

Parameters	Formulae
Moment [M] of a force	M = Fd
	$\sum M = 0$
Equilibrium conditions	$\sum F_{y} = 0$
	$\sum F_{x} = 0$
	$\Sigma CWM = \Sigma ACWM$
Equilibrium conditions (expanded)	$\Sigma F(up) = \Sigma F(down)$
	$\Sigma F(left) = \Sigma F(right)$

Selected derived SI units

	Derived SI units		
Derived quantities	Names Symbols Expression in terms of derived SI unit		
Force	newton	N	-
Pressure, stress	pascal	Pa	N m ⁻²
Energy, work	joule	J	N m

Common constant

Item	Symbol	Value
Gravity	g	9.80 m s ⁻²

Statics – second moment of area for material cross sections

Shapes	Dimensions	Second moment of area about centroidal axis
Vertical rectangle solid section	$x \xrightarrow{h} x$	$I_{xx} = \frac{bh^3}{12}$
Round solid section	x x	$I_{xx} = \frac{\pi D^4}{64}$
Circular tube section	D_o D_i D_i	$I_{xx} = \frac{\pi (D_o^4 - D_i^4)}{64}$

Terms:

 $b = \mathsf{base}$

D = diameter

 D_i = diameter (inside) D_i = diameter (outside) D_i = height

 $I_{\rm xx}$ = second moment of area for material cross sections

Statics - deflection of beams

Beam configurations	$\begin{array}{c} {\sf Maximum} \\ {\sf bending\ moment} \\ ({\it BM}_{\it max}) \end{array}$	Maximum deflection (y)
Cantilevered beam – single load at unsupported end		
$A \longrightarrow B$	$BM_{max} = FL$ at A	$y = \frac{FL^3}{3EI_{xx}} \text{ at } B$
Cantilevered beam – universally distributed load		
$F_{UDL} = \omega L$	$BM_{max} = \frac{F_{UDL}L}{2} \text{ at } A$	$y = \frac{F_{UDL}L^3}{8EI_{xx}} \text{ at } B$
Centrally loaded beam – simply supported at both		
ends F B C	$BM_{max} = \frac{FL}{4} \text{ at } C$	$y = \frac{FL^3}{48EI_{xx}} \text{ at } C$
Universally loaded beam – simply supported at both ends		
$A \qquad F_{UDL} = \omega L \qquad B$	$BM_{max} = \frac{F_{UDL}L}{8} \text{ at } C$	$y = \frac{5F_{UDL}L^3}{384EI_{xx}} \text{ at } C$

Terms:

E = elastic (Young's) modulus of the material of the beam

F = single vertical point load

 $\boldsymbol{F}_{\text{UDL}}$ = product of the UDL's applied load/unit length and the length of the beam

 I_{xx} = second moment of area of the beam section

 \vec{L} = length of beam between supports

 ω = uniformly distributed load per unit length

Dynamics formulae

Parameters	Formulae
Force [F]	F = ma
Acceleration [a]	$a = \frac{v - u}{t}$
Velocity [v]	$v^2 = u^2 + 2as$
Distance [s]	$s = ut + \frac{1}{2}at^2$
Work [W]	$W = F_S$
Power [P]	$P = \frac{F_S}{t} = F \overline{v}$
Potential energy $[E_p]$	$E_p = mgh$
Kinetic energy $[E_k]$	$E_k = \frac{1}{2} m v^2$
Energy conversion	$\Delta E_p = \Delta E_k$

Base International System (SI) units

Unit name	Unit abbreviation	Electrical parameter	Symbol	Expression in terms of derived SI units
ampere	А	Current	I	W V ⁻¹

Selected derived SI units

Unit names	Unit abbreviations	Electrical parameters	Symbols	Expression in terms of derived SI units
volt	V	Voltage	V	W A ⁻¹
ohm	Ω	Resistance	R	V A ⁻¹
farad	F	Capacitance	C	A s V ⁻¹
watt	W	Power	P	J s ⁻¹
hertz	Hz	Frequency	f	s ⁻¹

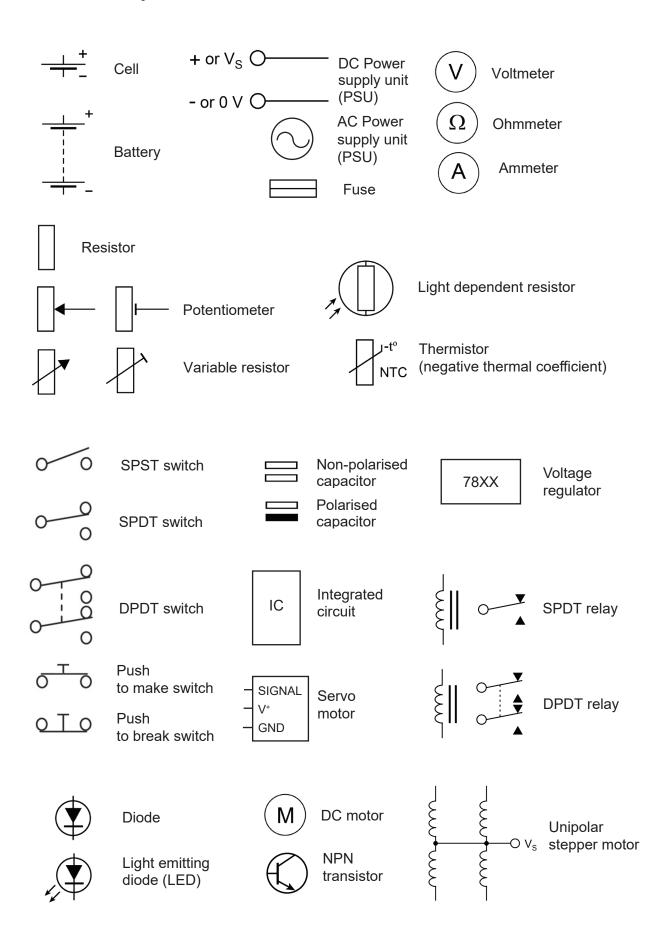
Law and principle formulae

Parameters	Formulae
Relationships between Ohm's law and power formula	$P = VI = I^2R = \frac{V^2}{R}$
Power [P]	$R = \frac{V}{I} = \frac{P}{P} = \frac{V^2}{P}$
Resistance [R]	
Voltage [V]	$V = IR = \frac{P}{I} = \sqrt{PR}$
Current [/]	$I = \frac{V}{R} = \frac{P}{V} = \sqrt{\frac{P}{R}}$
Electrical energy $[E_{_{arepsilon}}]$	$E_e = VIt$
Kirchhoff's first law	$\Sigma I = 0$
Kirchhoff's second law	$\Sigma \Delta V = 0$
Resistance [R] in series	$R_T = R_1 + R_2 + \cdots$
Resistance [R] in parallel	$\frac{1}{R_{T}} = \frac{1}{R_{1}} + \frac{1}{R_{2}} + \cdots$
Voltage dividers	$V_{cc} = V_{1} + V_{2}$ $V_{1} = V_{cc} \frac{R_{1}}{R_{1} + R_{2}}$ $V_{2} = V_{cc} \frac{R_{2}}{R_{1} + R_{2}}$
Resistor [R] in series with an LED	$R = \frac{V_{cc} - V_{LED}}{I_{LED}}$
Capacitance $[C]$ in series	$\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} + \cdots$
Capacitance $[C]$ in parallel	$C = C_1 + C_2 + \cdots$

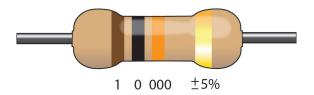
Mechanics formulae

Parameters	Formulae
Mechanical Advantage [MA]	$MA = \frac{load}{effort}$
Velocity Ratio [VR]	$VR = rac{d_{effort}}{d_{load}}$
Pulley belt ratio	$VR = rac{\mathcal{O} \text{ follower pulley}}{\mathcal{O} \text{ driver pulley}}$
Chain and sprocket ratio	$VR = \frac{n^o \text{ teeth follower gear}}{n^o \text{ teeth driver gear}}$
Gear ratio	$VR = \frac{n^o \text{ teeth follower gear}}{n^o \text{ teeth driver gear}}$
Velocity ratios [VR] for gear/pulley trains comprised of 3 or more gears/pulleys	$VR = \frac{F_1}{D_1} \frac{F_2}{D_2} \frac{F_3}{D_3} \dots$
Worm and worm wheel ratio	$VR = \frac{n^o teeth worm wheel}{1}$
Rack and pinion	$distance = \frac{n^o \text{ teeth pinion} \times revolutions}{n^o \text{ teeth per metre rack}}$
Linear velocity $[v]$ of belt or cable driven by pulley or drum	$v = \frac{(RPM) (2\pi r)}{60} = \frac{s}{t}$
Speed of rotation (r.p.m.)	Output speed (r.p.m.) = $\frac{Input \ speed \ (r.p.m.)}{VR}$

Standard circuit symbols



Resistor colour codes



Example: 4 band E12 series resistor colour code

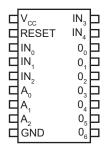
Band colours	1st band	2nd band	Multiplier	Tolerance band
Black	0	0	1	
Brown	1	1	10	1%
Red	2	2	100	2%
Orange	3	3	1000	
Yellow	4	4	10 000	
Green	5	5	100 000	
Blue	6	6	1 000 000	
Violet	7	7		
Grey	8	8		
White	9	9		
Gold				5%

E12 Preferred values:10, 12, 15, 18, 22, 27, 33, 39, 47, 56, 68, 82

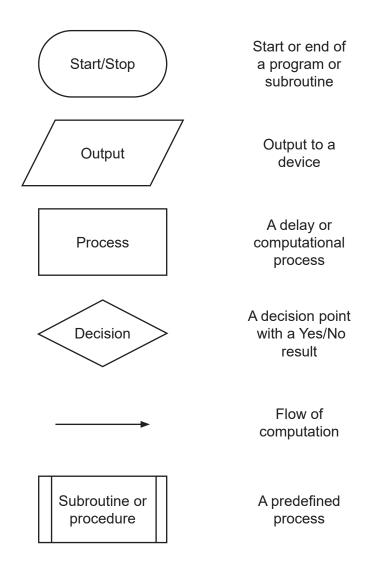
Diode and transistor

Diode model	Formulae	Diagram
On	$V_{_{D}} = V_{_{D,on}} (or \ V_{_{F}})$ Check: $I_{_{D}} > 0$	$\stackrel{I_D}{\longrightarrow}$
Off	$I_D = 0 A$ Check: $V_D < V_{D, on} (or V_F)$	anode (a) + V _D −
Transistor model (NPN BJT)	Formulae	Diagram
Cut-off	$I_{\rm B} = I_{\rm C} = 0~A$ Check: $V_{\rm BE} < 0.7~V$	
Saturation	$V_{BE}=0.7~V$ $V_{CE}=0~V$ Check: $I_{B}>0~A$ $\frac{I_{C}}{I_{B}}<\beta~(or~h_{FE})$	Collector I_{C} Base V_{CE} V_{BE}
Forward-active	$\begin{split} V_{_{BE}} &= 0.7 \ V \\ I_{_{C}} &= \beta \times I_{_{B}} \\ \textbf{Check:} \\ I_{_{B}} &> 0 \ A \\ V_{_{CE}} &> 0 \ V \end{split}$	$I_{\mathcal{E}}$ Emitter
Transistor current gain [β or h_{FE}]	$\beta = \frac{I_C}{I_B}$	

Standard microcontroller chip



Flow chart symbols



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