Government of Western Australia
School Curriculum and Standards Authority

## ENGINEERING STUDIES

## ATAR course examination 2018

## Marking Key

Marking keys are an explicit statement about what the examining panel expect of candidates when they respond to particular examination items. They help ensure a consistent interpretation of the criteria that guide the awarding of marks.

Part A: Multiple-choice

| 1 | b |
| :---: | :---: |
| 2 | c |
| 3 | d |
| 4 | c |
| 5 | a |
| 6 | d |
| 7 | b |
| 8 | d |
| 9 | a |
| 10 | b |

Part B: Extended response
Question 11


| Description |  | Marks |
| :---: | :---: | :---: |
| correct view (three faces - pictorial) |  | 1-3 |
|  | Sub-total | 3 |
| Common to either pictorial or orthographic view |  |  |
| external dimensions - all four correct |  | 1-4 |
| neatness overall |  | 1 |
|  | Sub-total | 5 |
| If uses pictorial view |  |  |
| length, width and depth in proportion |  | 1-2 |
| correct position and proportion of the rectangular slot |  | 1-2 |
| correct position and proportion of holes |  | 1-2 |
| correct position and proportion of semi-circular opening |  | 1 |
|  | Sub-total | 7 |
| If uses orthographic view |  |  |
| length and width full size |  | 1-2 |
| correct position and size of the rectangular slot |  | 1-2 |
| correct position and size of holes as hidden detail |  | 1-2 |
| correct position and size of semi-circular opening as hidden detail |  | 1 |
|  | Sub-total | 7 |
|  | Total | 15 |

## Question 12

Complete the table below by naming the material you have studied this year that is most suitable for each of the given applications and give one reason why that material is fit for purpose.

| Description | Marks |  |  |
| :--- | :---: | :---: | :---: |
| One mark per correct material and one mark for fitness of purpose | 1 |  |  |
| names a suitable material for application | 1 |  |  |
| states reason material is fit for purpose | Subtotal |  |  |
| $\mathbf{2}$ |  |  |  |
| Accept other relevant answers | $\mathbf{1 2}$ |  |  |


| Application | Material | Fitness for purpose |
| :--- | :--- | :--- |
| frames and supports for <br> solar panels | aluminium | non-corrosive, malleable, <br> strong |
| tubing on the panels of <br> solar hot water systems | copper | excellent conductor of heat, <br> ductile |
| fibre optic cable | acrylic fibre | easy to bend, internally <br> reflects light |
| lenses in protective glasses | polycarbonate | impact resistant, hard to <br> crack |
| metal coating the surface of <br> structural steel | zinc | stops iron from corroding by <br> forming a (oxide) coating on <br> the surface that does not <br> flake off |
| 3D printer filament | acrylonitrile butadiene (ABS) | relatively low melting point, <br> hard setting |

Question 13
(a) Calculate the volume of metal in one of these cables.

| Description | Marks |
| :---: | :---: |
| $\mathrm{R}=0.0125 \mathrm{~m}$ | 1 |
| $\mathrm{~V}=\pi \mathrm{R}^{2} \mathrm{I}$ |  |
| $=\pi \times 0.0125^{2} \times 560$ | 1 |
| $=0.2749 \mathrm{~m}^{3}$ | Total |
|  | $\mathbf{3}$ |

(b) Determine the total mass of steel in all six cables.

| Description |  | Marks |
| :---: | :---: | :---: |
| Density $=7850 \mathrm{~kg} \mathrm{~m}^{3}$ |  | 1 |
| $\begin{aligned} \text { Mass } & =\text { density } \times \text { volume } \\ & =7850 \times 0.2749 \times 6 \end{aligned}$ |  | 1 |
| $=12948 \mathrm{~kg}$ |  | 1 |
|  | Total | 3 |

(c) Calculate the length of the cable between the terminals when the carriage is centrally located across the gap. A diagram is required in your answer.
(5 marks)

| Description |  |  |  |
| :--- | :---: | :---: | :---: |
| 540 m |  |  | Marks |
| vertical drop in centre of cable $=73-60=13 \mathrm{~m}$ | 1 |  |  |
| $\mathrm{~L}^{2}=(540 / 2)^{2}+13^{2}=73069$ | 1 |  |  |
| $\mathrm{~L}=270.3 \mathrm{~m}$ | 1 |  |  |
| length of cable $=2 \times 270.3=540.6=541 \mathrm{~m}$ | 1 |  |  |
|  | 1 |  |  |

(d) Explain, including a relevant calculation, why each counterweight has a mass of 10 tonnes.

| Description | Marks |
| :--- | :---: |
| maximum downwards weight on cable when carriage is at the centre | 1 |
| weight of cable + weight of car $=12.9+7=19.9$ tonne | 1 |
| downwards weight on each end needs to equal (or slightly exceed) half of <br> this value therefore ten tonne each end will do this | 1 |
| Total |  |
| Accept other relevant answers | $\mathbf{3}$ |

(e) Calculate the energy expended per round trip in joules.

| Description | Marks |  |
| :--- | :--- | :---: |
| Energy $=\mathrm{Pt}$ |  |  |
| $0.75 \mathrm{E}=\mathrm{Pt}$ | 1 |  |
| E | $=(57000 \times 4.7 \times 60 \times 2) / 0.75$ | 1 |
| $=4.286 \times 10^{7} \mathrm{~J}$ |  | 1 |
|  | Total | $\mathbf{3}$ |

(a) The glass and aluminium greenhouse is being set onto a 75 mm thick concrete pad which is the exact size of the footprint of the greenhouse. Calculate the volume of concrete required in cubic metres.
(3 marks)

| Description | Marks |  |
| :--- | :---: | :---: |
| Area $=(4.3 \times 3.4)-(1.1 \times 1.3 \times 2)$ | 1 |  |
| Volume $=11.76 \mathrm{~m}^{2}$ | $=11.76 \times 0.075=0.882 \mathrm{~m}^{3}$ | 1 |
|  | Total | $\mathbf{3}$ |

(b) Give two reasons why steel is the preferred material for securing the greenhouse.
(2 marks)

| Description |  | Marks |
| :---: | :---: | :---: |
| Any two of: <br> - strong <br> - resists deformation <br> - high tensile strength. |  | 1-2 |
|  | Total | 2 |
| Accept other relevant answers |  |  |

(c) Calculate the length of cable required for all three gable ends assuming that each cable needs an extra 100 mm in length to tie it to a peg on either side.

(d) When the greenhouse is no longer required state how the following materials can be disposed of and what happens to them if they are recycled.
(i) Glass

| Description | Marks |
| :--- | :---: |
| disposed of in general waste at a general rubbish tip | 1 |
| separated from waste then crushed, melted down and remoulded <br> into bottles or jars | 1 |
| Total |  |
| Accept other relevant answers | $\mathbf{2}$ |

(ii) Concrete pad

| Description | Marks |
| :--- | :---: |
| disposed of as clean landfill (not general rubbish tip) | 1 |
| crushed and recycled as road-base | 1 |
| Accept other relevant answers |  |

## Part A: Multiple-choice

10\% (10 Marks)

| 15 | d |
| :---: | :---: |
| 16 | a |
| 17 | b |
| 18 | c |
| 19 | c |
| 20 | d |
| 21 | b |
| 22 | a |
| 23 | d |
| 24 | d |

## Part B: Extended answer

Question 25
(a) How far from the top of the vertical support is the stainless steel cable AD attached?

| Description | Marks |  |
| :--- | :---: | :---: |
| $\mathrm{BD}^{2}=\mathrm{AD}^{2}-\mathrm{AB}^{2}$ <br> $=2.40^{2}-2.00^{2}=1.76$ | 1 |  |
| $\mathrm{BD}=1.33 \mathrm{~m}$ | Total | $\mathbf{2}$ |

(b) Calculate the second moment of area for this horizontal beam.

| Description | Marks |
| :--- | :---: |
| $\mathrm{I}_{\mathrm{xx}}$ $=\mathrm{bh}^{3} / 12$ <br> $=0.03 \times 0.07^{3} / 12$  | $1-2$ |
| $=8.575 \times 10^{-7}\left(\right.$ answer must be in $\mathrm{m}^{4}$ or $\left.\mathrm{mm}^{4}\right)$ | 1 |
|  | Total |

(c) Calculate the maximum bending moment of the beam at $B$ before the sign is attached. (Assume the section AB remains horizontal and there is no significant bending in the vertical support.)
$\left.\begin{array}{|l|c|c|}\hline & \text { Description } & \text { Marks } \\ \hline \text { FudL } & =(148 \times 9.8 / 9) \times 7 \\ & =1128 \mathrm{~N}\end{array}\right)$
(d) Calculate the maximum deflection of the beam at $C$ before the sign is attached. (Assume the section $A B$ remains horizontal and there is no significant bending in the vertical support.)

| Description |  | Marks |
| :---: | :---: | :---: |
| $\begin{aligned} \text { yb } & =\mathrm{FudLL}^{3} / 8 \mathrm{EI}_{\times x} \\ & =\left(161.2 \times 7^{3}\right) /\left(8 \times 2 \times 10^{11} \times 8.575 \times 10^{-7}\right) \end{aligned}$ |  | 1-3 |
| $=0.0403 \mathrm{~m}$ |  | 1 |
|  | Total | 4 |

(e) Calculate the maximum deflection of the beam at C when the sign is attached. (Assume the section $A B$ remains horizontal and there is no significant bending in the vertical support.) If you were unable to obtain a value for part (d), use 0.0500 m .

| Description | Marks |  |
| :--- | :---: | :---: |
| $\mathrm{y}_{\mathrm{C}}$ | $=\mathrm{y}_{\mathrm{B}}+\mathrm{FL}^{3} / 3 \mathrm{EI}_{\mathrm{xx}}$ |  |
|  | $=0.0403+\left(60 \times 9.8 \times 5.5^{3}\right) /\left(3 \times 2 \times 10^{11} \times 8.575 \times 10^{-7}\right)$ | $1-2$ |
|  | $=0.0403+0.01941$ |  |
|  | $=0.0597 \mathrm{~m}(0.0694)$ | 1 |
|  | Total | $\mathbf{4}$ |

(f) Calculate the tension in the cable AD assuming the beam AC is horizontal. (5 marks)

| Description | Marks |
| :---: | :---: |
| Moments about B |  |
| Sum acm = sum cm |  |
| $\mathrm{T}_{\text {cable }} \sin 33.6^{\circ} \times 2=148 \times 9.8 \times 2.5+60 \times 9.8 \times 5.5$ | 1-3 |
| $\mathrm{T}=(3626+3242) / 1.107$ | 1 |
| $=6204 \mathrm{~N}$ | 1 |
|  |  |

Question 26
(a) Calculate the length of the ramp XP.

| Description | Marks |
| :---: | :---: |
| $X P=28 / \sin 38^{\circ}$ | 1 |
| $=45.48 \mathrm{~m}$ | 1 |
|  | Total |

(b) Calculate the time it takes for the roller-coaster to travel from X to P ?

| Description | Marks |  |
| :--- | :---: | :---: |
|  $=\mathrm{s} / \mathrm{V}_{\mathrm{av}}$ <br>  $=45.48 / 0.72$ | 1 |  |
|  | $=63.17 \mathrm{~s}$ | Total |
|  | $\mathbf{2}$ |  |

(c) A person in the car when stationary at point P dropped a 150 g chocolate bar. How long would it take to hit the ground, assuming that it fell from the person's hand when it was 28.5 m above the ground? (Ignore any resistance.)
(3 marks)

| Description | Marks |  |
| :--- | :---: | :---: |
| $\mathrm{s}=\mathrm{ut}+0.5 \mathrm{at}^{2}$ |  |  |
| $28.5=0+0.5 \times 9.8 \mathrm{t}^{2}$ | 1 |  |
| $\mathrm{t}=\sqrt{\frac{28.5}{4.9}}=\sqrt{5.81}$ | 1 |  |
| $\mathrm{t}=2.41 \mathrm{~s}$ |  | 1 |
|  | Total | $\mathbf{3}$ |

(d) Calculate the frictional force between the track and the car.
(2 marks)

| Description | Marks |
| :--- | :---: |
| \begin{tabular}{rl\|}
\hline
\end{tabular}$=0.15 \mathrm{mg}$ |  |
| $=0.15 \times 1600 \times 9.8$ | 1 |
|  | $=2352 \mathrm{~N}$ |
|  | Total |

(e) Using this information calculate the force the motor must apply to the car to move it up this slope at a constant velocity.

| Description |  | Marks |
| :---: | :---: | :---: |
| $\mathrm{F}=\mathrm{mgsin} 38^{\circ}+\mathrm{F}_{\mathrm{f}}$ |  | 1 |
| $\begin{aligned} & =1600 \times 9.8 \times \sin 38+2352 \\ & =9654+2352 \end{aligned}$ |  | 1-2 |
| $=12006 \mathrm{~N}$ |  | 1 |
|  | Total | 4 |

(f) Determine the power rating of the motor used to achieve this task, if it is $80 \%$ efficient. If you were unable to obtain a value for part (e), use 11000 N .
(2 marks)

| Description | Marks |  |
| :--- | :---: | :---: |
| $0.8 \mathrm{P}=\mathrm{FV}_{\text {av }}$ | 1 |  |
| P$=12006 \times 0.72 / 0.8$  <br>  $10805 \mathrm{~W}(9900 \mathrm{~W})$ | 1 |  |
|  | Total | $\mathbf{2}$ |

(a) Indicate the direction of the car's acceleration in each of the following regions by circling the correct answer either up or down.

|  | Description |
| :--- | :---: |
| (i) down Marks |  |
| (ii) down | 1 |
|  | 1 |

(b) Explain the reasoning you used to choose your answer for (a)(ii) above.
(2 marks)

| Description | Marks |
| :--- | :---: |
| only acceleration on the car is due to a component of gravity | 1 |
| gravity is always vertically downwards | 1 |
|  | $\mathbf{2}$ |

(c) Calculate the speed of the roller-coaster car at point $Q$, assuming there is no energy losses between $P$ and $Q$ and $P Q$ is a straight line.
(3 marks)

| Description | Marks |
| :---: | :---: |
| $0.5 \mathrm{mv}^{2}=\mathrm{mgh}$ | 1 |
| $\mathrm{v}=\sqrt{2 g h}$ <br> $=\sqrt{2 \times 9.8 \times 28}$ | 1 |
| $=23.43 \mathrm{~ms}^{-1}$ | Total |
|  | $\mathbf{3}$ |

(d) Calculate the amount of energy 'lost' by the roller-coaster car between $P$ and $Q$ if its actual speed at $Q$ is $20.6 \mathrm{~ms}^{-1}$.
(2 marks)

| Description | Marks |
| :--- | :---: |
| $\mathrm{E}_{\mathrm{K}}$ $=0.5 \mathrm{mv}^{2}-0.5 \mathrm{mu}^{2}$ <br> $=0.5 \times 1600 \times\left[(23.43)^{2}-(20.6)^{2}\right]$  | 1 |
|  | $=99684 \mathrm{~J}=9.97 \times 10^{4} \mathrm{~J}$ |$\quad$ Total | $\mathbf{2}$ |
| :--- |

(e) With regard to this 'lost' energy:
(i) State the form of energy into which most of it is transformed.

| Description | Marks |
| :---: | :---: |
| Heat | 1 |
|  | Total |

(ii) State where this transformed energy immediately goes.

| Description | Marks |  |
| :--- | :---: | :---: |
| into the rails/wheels of car | 1 |  |
|  | Total | $\mathbf{1}$ |
| Accept other relevant answer |  |  |
|  |  |  |

(f) Determine the proportion of the roller-coaster car's potential energy 'lost' by the time it reaches point Q ?
(4 marks)

| Description |  | Marks |
| :---: | :---: | :---: |
| $\begin{aligned} E_{p} \text { at start } & =m g h \\ & =1600 \times 9.8 \times 28 \\ & =4.39 \times 10^{5} \mathrm{~J} \end{aligned}$ |  | 1 |
| $\begin{aligned} 0.5 \mathrm{mv}^{2} & =0.5 \times 1600 \times 20.6^{2} \\ & =3.39 \times 10^{5} \end{aligned}$ |  | 1 |
| Proportion lost $=(4.39-3.39) / 4.39$ |  | 1 |
| = 0.228 or $22.8 \%$ |  | 1 |
|  | Total | 4 |

(g) If this same proportion of energy is 'lost' as kinetic energy between $Q$ and $R$, determine the maximum height of $R$ above $Q$. If you were unable to obtain a value for part ( $f$ ) use 25\%.

(a) Name the structural part of this crane that will be under compression.

| Description | Marks |  |
| :---: | :---: | :---: |
| Jib | 1 |  |
|  | Total | 1 |

(b) Determine the minimum radius of each of the steel lifting cables needed to lift a container filled with its maximum weight just before each cable undergoes plastic deformation.

| Description |  | Marks |
| :---: | :---: | :---: |
| Force per cable $=(27300 \times 9.8) / 2$ |  | 1 |
| $=133770 \mathrm{~N}$ |  | 1 |
| $\begin{aligned} \hline \text { Yield stress } & =250 \times 10^{6} \mathrm{Nm}^{-2} \text { (from data book) } \\ \text { Stress } & =\text { F/A } \end{aligned}$ |  | 1 |
| $\begin{aligned} \mathrm{A} & =\mathrm{F} / \text { stress } \\ & =133770 /\left(250 \times 10^{6}\right) \\ & =5.35 \times 10^{-4} \mathrm{~m}^{2} \text { per cable } \end{aligned}$ |  | 1 |
| $\begin{aligned} & A=\pi R^{2} \\ & r^{2}=5.35 \times 10^{-4} / \pi \end{aligned}$ |  | 1 |
| $r=0.01305 \mathrm{~m}$ |  | 1 |
|  | Total | 6 |

(c) Using $540 \mathrm{~mm}^{2}$ as the cross sectional area for each lifting cable, determine the mass of the load that would need to be attached to cause these cables to break if an attempt was made to lift the container.
(4 marks)

| Description |  | Marks |
| :---: | :---: | :---: |
| $\begin{aligned} & \text { UTS }=470 \times 10^{6} \mathrm{Nm}^{-2} \text { (from data book) } \\ & \text { UTS }=\text { F/A } \end{aligned}$ |  | 1 |
| $\begin{aligned} \mathrm{F} & =\text { UTS } \times \text { A } \\ & =470 \times 10^{6} \times 540 \times 10^{-6} \times 2 \end{aligned}$ |  | 1 |
| $=507600 \mathrm{~N}$ |  | 1 |
| $\begin{aligned} \text { Mass } & =\mathrm{F} / \mathrm{g} \\ & =507600 / 9.8 \\ & =51797 \mathrm{~kg}=51800 \mathrm{~kg} \end{aligned}$ |  | 1 |
|  | Total | 4 |

(d) State two situations that could arise in lifting a load requiring a factor of safety to be applied to the steel lifting cables.

| Description | Marks |
| :--- | :---: |
| cross winds when lifting | 1 |
| any sudden movement of the load | 1 |
| Accept other relevant answers | $\mathbf{2}$ |

(e) Calculate the increase in length of each steel lifting cable under this load at the point the container just started to rise from the wharf.
(4 marks)

| Description | Marks |  |
| :--- | :---: | :---: |
| $\mathrm{E}=\mathrm{FL} / \mathrm{A} \Delta \mathrm{L}$ | 1 |  |
| $\Delta \mathrm{~L}=\mathrm{FL} / \mathrm{EA}$ |  |  |
| $=(88000 \times 40) /\left(2 \times 10^{11} \times \pi \times\left(4.15 \times 10^{-2}\right)^{2}\right.$ | $1-2$ |  |
| $=3.25 \mathrm{~mm}(0.00325 \mathrm{~m})$ | Total | $\mathbf{4}$ |

## Question 29

(a) Calculate the downward force on the tow ball of the car when the trailer with boat and motor are attached to the car. The tow ball is the contact point between the boat trailer and the car.

| Description |  | Marks |
| :---: | :---: | :---: |
| $\begin{aligned} & \sum \mathrm{acm}=\Sigma \mathrm{cm} \\ & \mathrm{rF} \mathrm{motor}_{\text {mor }}+\mathrm{rF} \\ & \text { hitch } \end{aligned}=\mathrm{rF} \text { boat+trailer }$ |  | 1 |
| $(1.2 \times 112 \times 9.8)+(2.5 \times F)=0.50 \times 540 \times 9.8$ |  | 1-2 |
| $\begin{aligned} \mathrm{F}_{\text {hitch }} & =1328.88 / 2.5 \\ & =531.5 \mathrm{~N} \end{aligned}$ |  | 1 |
|  | Total | 4 |

(b) The power output of boat motors is almost exclusively measured using the unit of Horsepower ( Hp ). Given the power of this motor is 60 Hp , convert this into kilowatts given $1 \mathrm{Hp}=746 \mathrm{~W}$.

| Power $=60 \times 746 / 1000$ <br> $=44.76 \mathrm{~kW}$  | Description | Marks |
| :---: | :---: | :---: |
|  | Total | 1 |

(c) Calculate the tension in the cable when it is parallel to the ramp. You are required to give the correct units in your answer.
(4 marks)

| Description | Marks |
| :--- | :---: |
| Total mass $=400+112=512 \mathrm{~kg}$ | 1 |
|  $=\mathrm{mg} \operatorname{Sin} \theta$ <br> $=512 \times 9.8 \times \operatorname{Sin} 20$  | $1-2$ |
| $=1716 \mathrm{~N}$ (unit must be correct for this mark) | Total |
|  | $\mathbf{4}$ |

(d) Suggest a suitable material for construction of the trailer. Give two reasons why this material was chosen.
(3 marks)

| Description | Marks |
| :--- | :---: |
| suitable materials either aluminium or galvanised iron | 1 |
| Any two of: <br> • good corrosion resistance <br> strong <br> easy to work with |  |
| Accept other relevant answers |  |
| Total |  |

## Question 30

(a) Calculate the upward force required by each motor to enable the drone to hover at a constant height. Assume the drone does not lose any power during the flight and there are no external wind factors.

| F $\quad$ ma Description |  | Marks |
| :---: | :---: | :---: |
| F | $\begin{aligned} & =\mathrm{ma} \\ & =0.734 \times 9.8=7.19 \mathrm{~N} \end{aligned}$ | 1 |
| $\begin{array}{\|l\|} \hline \text { Fup } \\ \mathrm{F} \times 4 \end{array}$ | $\begin{aligned} & =\mathrm{F}_{\text {fown }} \\ & =7.19 \\ & =7.19 / 4 \end{aligned}$ | 1 |
| $\mathrm{F}_{\text {each motor }}=1.80 \mathrm{~N}$ |  | 1 |
|  |  | 3 |

(b) Using the maximum ascent, controlled descent and flight times, calculate the maximum height to which the drone can fly. Ignore any acceleration a deceleration effects.
(4 marks)

| Description |  | Marks |
| :---: | :---: | :---: |
| $\begin{array}{\|ll} \hline \mathrm{t} & =27 \times 60 \\ & =1620 \mathrm{~s} \end{array}$ |  | 1 |
| $\begin{array}{\|ll} \hline v \quad=s / t \\ t & =s / v \\ 1620 & =s / 5+s / 3 \end{array}$ |  | 1 |
| $1620=(3 s+5 s) / 15$ |  | 1 |
| $\mathrm{s} \quad=3037 \mathrm{~m}$ |  | 1 |
|  | Total | 4 |

(c) Calculate the total time that the drone would take to ascend to 100 m , fly to the maximum range, return and perform a controlled descent to the ground, all at maximum speed. (Assume maximum speed is reached immediately on liftoff.)

| Description |  | Marks |
| :---: | :---: | :---: |
| Ascent |  |  |
| $\begin{aligned} & \mathrm{t}=\mathrm{s} / \mathrm{v}=100 / 5 \\ & =20 \text { seconds } \end{aligned}$ |  | 1 |
| Horizontal |  |  |
| $\begin{aligned} & s=13000 \times 2 \\ & =26000 \mathrm{~m} \end{aligned}$ |  | 1 |
| Convert velocity to $\mathrm{ms}^{-1}$ $\begin{aligned} & v=65 / 3.6 \\ & =18.05 \mathrm{~ms}^{-1} \end{aligned}$ |  | 1 |
| $\begin{aligned} & t=s / v \\ & =26000 / 18.05 \\ & =1440 \mathrm{~s} \end{aligned}$ |  | 1 |
| Descent |  |  |
| $\mathrm{t}=\mathrm{s} / \mathrm{v}=100 / 3=33.3 \mathrm{~s}$ |  | 1 |
| Total time $=20+1440+33.3=1493 \mathrm{~s}$ or 24.9 min |  | 1 |
|  | Total | 6 |

## Question 30 (continued)

(d) The drone's camera is pointed vertically downward and takes square photographs. Calculate the surface area of land that it could photograph at a height of 100 m , given that a field of view of $78.8^{\circ}$ means the angle of view to the vertical is $39.4^{\circ}$. (3 marks)

| Description | Marks |
| :--- | :---: |
| Length of base $=100 \tan \theta \times 2=164.3 \mathrm{~m}$ | $1-2$ |
| Area $=164.3^{2}=26994 \mathrm{~m}^{2}$ | 1 |
|  | Total |

Part A: Multiple-choice
10\% (10 Marks)

| 31 | b |
| :---: | :---: |
| 32 | b |
| 33 | a |
| 34 | c |
| 35 | d |
| 36 | c |
| 37 | a |
| 38 | a |
| 39 | c |
| 40 | d |

Part B: Extended answer
50\% (100 Marks)
Question 41
(a) Calculate the voltage and the current capacity of this battery pack at the outputs $A B$.
(2 marks)

| Description | Marks |
| :--- | :---: |
| $4.5 \mathrm{~V}+4.5 \mathrm{~V}=9 \mathrm{~V}$ | 1 |
| 2 A | 1 |
|  | Total |

(b) Determine the voltage and current capacity this cell would need to have so that this battery pack could supply 6 A at 4.5 V to the load.
(2 marks)

| Description | Marks |
| :--- | :---: |
| 4.5 V | 1 |
| $6 \mathrm{~A}-2 \mathrm{~A}-3 \mathrm{~A}=1 \mathrm{~A}$ | 1 |
|  | Total |

(c) Calculate the minimum Ah that the third cell connected between $A$ and $B$ must have to achieve this.

| Description |  | Marks |
| :---: | :---: | :---: |
| Load |  |  |
| $\begin{aligned} & 1.2 \mathrm{~A} \times 100 \mathrm{~h} \\ & =120 \mathrm{Ah} \end{aligned}$ |  | 1 |
| Duty Cycle |  |  |
| $\begin{aligned} & 120 \mathrm{Ah} * 0.8 \\ & =96 \mathrm{Ah} \end{aligned}$ |  | 1 |
| Existing cells |  |  |
| $\begin{aligned} & 50 \mathrm{Ah}+30 \mathrm{Ah} \\ & =80 \mathrm{Ah} \end{aligned}$ |  | 1 |
| Required cells |  |  |
| $\begin{aligned} & =96 \mathrm{Ah}-80 \mathrm{Ah} \\ & =16 \mathrm{Ah} \text { minimum } \end{aligned}$ |  | 1 |
|  | Total | 4 |

Question 41 (continued)
(d) Calculate the total capacitance across AB in the circuit below.
(3 marks)

| Description |  | Marks |
| :---: | :---: | :---: |
| $4700 \mathrm{nF}=4.7 \mu \mathrm{~F}$ |  | 1 |
| $\begin{aligned} \hline \text { Cs } & =1 /\left(\frac{1}{4}+\frac{1}{4.7}\right) \\ & =2.16 \mu \mathrm{~F} \end{aligned}$ |  | 1 |
| $\begin{aligned} \mathrm{C}_{\mathrm{a}, \mathrm{~b}} & =2.16 \mu \mathrm{~F}+5 \mu \mathrm{~F} \\ & =7.16 \mu \mathrm{~F} \end{aligned}$ |  | 1 |
|  | Total | 3 |

(e) Calculate the value of the capacitor required to bring the total capacitance between A and $B$ in the circuit above to $10 \mu \mathrm{~F}$ and correctly draw it into the circuit in part (d).
(2 marks)


## Question 42

(a) Complete the table below identifying the components in the circuit.

| Description |  | Marks |
| :---: | :--- | :---: |
| Diagram label | Component |  |
| Vcc | DC voltage source/9 V battery | 1 |
| T1 | NPN transistor | 1 |
| C1 | (polarised) capacitor | 1 |
| L1 | LED | 1 |
| R1 | Resistor | 1 |
| S1 | Switch | 1 |
| $\quad$ Total |  | $\mathbf{6}$ |

(b) Determine the initial value of the current i0 with switch S 1 open.

|  | Description | Marks |
| :--- | :---: | :---: |
| $\mathrm{i} 0=0$ | Total | 1 |
|  | $\mathbf{1}$ |  |

(c) Explain what happens to the current i 1 and i 2 over time when the switch S 1 is closed.

| Description | Marks |  |
| :--- | :---: | :---: |
| initially i1 is large and i2 is small as C1 charges | 1 |  |
| as C1 approaches full charge i2 approaches i0 | 1 |  |
|  |  |  |
| Accept other relevant answers | $\mathbf{2}$ |  |

(d) Explain what happens to the mode of T1 when the switch S 1 is closed?

| Description | Marks |  |  |
| :--- | :---: | :---: | :---: |
| starts in cut off | 1 |  |  |
| goes to forward active | 1 |  |  |
| Total |  |  | $\mathbf{2}$ |
| Accept other relevant answers |  |  |  |

(e) If C1 was reduced, what effect would this have on L1? State the reason for your answer.
(2 marks)

| Description | Marks |  |  |
| :--- | :---: | :---: | :---: |
| L1 would reach full brightness faster | 1 |  |  |
| because the capacitor C1 would reach full charge faster | 1 |  |  |
| Total |  |  | $\mathbf{2}$ |
| Accept other relevant answers |  |  |  |

(f) With reference to voltages $\mathrm{V}_{\mathrm{E}}, \mathrm{V}_{\mathrm{B}}$ and $\mathrm{V}_{\mathrm{C}}$, how can we determine that T 1 cannot go into saturation mode?

| Description | Marks |  |  |
| :--- | :---: | :---: | :---: |
| for saturation $\mathrm{V}_{\mathrm{B}}>\mathrm{V}_{\mathrm{C}}$ in NPN transistor | 1 |  |  |
| $\mathrm{~V}_{\mathrm{B}}$ cannot be greater than $\mathrm{V}_{\mathrm{C}}$ due to the voltage drop across R1 of Vcc | 1 |  |  |
| Total |  |  | $\mathbf{2}$ |
| Accept other relevant answers |  |  |  |

## Question 43

(a) Explain how you would measure the current flowing from the voltage source into the $1 \mathrm{k} 2 \Omega$ resistor.
(3 marks)

| Description | Marks |
| :--- | :---: |
| use an ammeter or multi-meter set to measure current | 1 |
| break the circuit and insert the meter in series | 1 |
| at points M and B (L \& K are also acceptable) | 1 |
| Total |  |
| Note: if uses calculation of current only then award a maximum of 2 marks |  |

(b) Calculate the maximum possible total resistance of the circuit.

| Description | Marks |
| :--- | :---: |
| $\mathrm{R}_{\mathrm{BC}, \mathrm{MAX}}=1200 \Omega+0.1 \times 1200 \Omega=1320 \Omega$ |  |
| $\mathrm{R}_{\text {FH, MAX }}=2200 \Omega+0.1 \times 2200 \Omega=2420 \Omega$ |  |$)$

(c) Calculate the minimum possible total resistance of the circuit.

| Description |  | Marks |
| :---: | :---: | :---: |
| $\begin{aligned} & \mathrm{R}_{\mathrm{BC}, \mathrm{MIN}}=1200 \Omega-0.1 \times 1200 \Omega=1080 \Omega \\ & \mathrm{R}_{\mathrm{FH}, \mathrm{MI}}=2200 \Omega-0.1 \times 2200 \Omega=1980 \Omega \end{aligned}$ |  | 1-2 |
| $\begin{aligned} & \mathrm{R}_{\mathrm{EG}, \mathrm{MIN}}=800 \Omega-0.05 \times 800 \Omega=760 \Omega \\ & \mathrm{R}_{\mathrm{GJ}, \mathrm{MIN}}=3300 \Omega-0.05 \times 3300 \Omega=3135 \Omega \\ & \hline \end{aligned}$ |  | 1-2 |
| $\begin{aligned} R_{E J, M I N} & =R_{E G, M I N}+R_{G J, M I N} \\ & =760 \Omega+3135 \Omega \\ & =3895 \Omega \end{aligned}$ |  | 1 |
| $\begin{aligned} \mathrm{R}_{\mathrm{DK}, \mathrm{MIN}} & =1 /\left(\left(1 / \mathrm{R}_{\text {FH, MIN }}\right)+\left(1 / \mathrm{R}_{\mathrm{EJ}, \mathrm{MIN}}\right)\right) \\ & =1 /((1 / 1980 \Omega)+(1 / 3895 \Omega)) \\ & =1313 \Omega \end{aligned}$ |  | 1 |
| $\begin{aligned} \mathrm{R}_{\mathrm{T}, \mathrm{MIN}} & =\mathrm{R}_{\mathrm{BC}, \mathrm{MIN}}+\mathrm{R}_{\mathrm{DK}, \mathrm{MIN}} \\ & =1080 \Omega+1313 \Omega \\ & =2393 \Omega \text { (to the nearest Ohm) } \end{aligned}$ |  | 1 |
|  | Total | 7 |
| Not all working is required. |  |  |

(d) Calculate the maximum possible current flowing at i1. If you were unable to obtain an answer for part (c), use $\mathrm{R}_{\mathrm{T} \text { MIN }}=2600 \Omega$.

| Description |  | Marks |
| :---: | :---: | :---: |
| Maximum current $\begin{aligned} & \mathrm{i}_{\mathrm{MAX}}=\mathrm{V}_{\mathrm{CC}} / \mathrm{R}_{\mathrm{T}, \mathrm{MIN}} \\ & \mathrm{i} 1_{\text {MAX }}=12 \mathrm{~V} / 2393 \Omega \\ & \mathrm{i} 1_{\text {MAX }}=5.0 \mathrm{~mA}(4.6 \mathrm{~mA}) \end{aligned}$ |  | 1 |
|  | Total | 1 |

(e) Calculate the maximum possible power dissipated by the $1 \mathrm{k} 2 \Omega$ resistor. If you were unable to obtain an answer for part (d), use i1 $1_{\text {max }}=4.6 \mathrm{~mA}$.

| Description | Marks |
| :--- | :---: |
| Maximum power |  |
| $\mathrm{P}_{\mathrm{BC}, \mathrm{MAX}}=\left(\mathrm{i} 1 \mathrm{MAX}^{2}\right) \mathrm{R}_{\mathrm{BC}, \text { min }}$ |  |
| $\mathrm{P}_{\mathrm{BC}, \mathrm{MAX}}=(0.0050)^{2} \times 1080$ |  |
| $\mathrm{P}_{\mathrm{BC}, \mathrm{MAX}}=27 \mathrm{~mW}(22.8 \mathrm{~mW})$ |  |
|  | Total |

(a) Name one advantage and one disadvantage of an open loop control system. (2 marks)

| Description | Marks |
| :--- | :---: |
| Advantages |  |
| Any of the following: <br> - simple/economical <br> - easy to maintain | 1 |
| Disadvantages |  |
| Any of the following:  <br> Q inaccurate/output is not monitored  <br> - unreliable  <br> cannot remove external disturbances  | 1 |
| Accept other relevant answers |  |

(b) Name one advantage and one disadvantage of a closed loop control system. (2 marks)

| Description | Marks |
| :--- | :---: |
| Advantages |  |
| Any of the following: <br> - accurate <br> - can remove external disturbances | 1 |
| Disadvantages |  |
| Any of the following:  <br> - stability issues  <br> - tumplex/uneconomical  <br> tuning/maintenance costs  | 1 |
| Accept other relevant answers |  |

(c) Complete the table below by identifying what should be at each of the labelled locations of the control system above.

| Description |  | Marks |
| :---: | :--- | :---: |
| A | desired speed (input)/set point | 1 |
| B | error | 1 |
| C | motor command | 1 |
| D | DC motor/plant | 1 |
| E | disturbances/power supply for motor | 1 |
| F | actual speed (output) | 1 |
| G | encoder/tachometer/feedback sensor | 1 |
| H | measured signal | 1 |
| Accept other relevant answers |  | $\mathbf{8}$ |

## Question 45

(a) The control system below will use a N/O switch S 1 as an input that will later be programmed to turn on a motor. It will also have a N/C switch S2 connected as an input that will be programmed to be used for directional control of the motor. Draw the wiring diagram for this below. The input pins have internal pull up resistors that can be assumed to have been programmed to be on.


| Description | Marks |
| :--- | :---: |
| switch 1 symbol correct and marked S1 | 1 |
| Switch 2 symbol correct and marked S2 | 1 |
| S1 and S2 connected to input pins on one side | 1 |
| S1 and S2 connected to ground on other side (either GND) | 1 |
|  | Total |

Question 45 (continued)
(b) The control system below will use an output to turn on a LED L1 with a resistor R1 in series. This will later be programmed to turn on when the motor is running. Draw the wiring diagram for this below.


| Description | Marks |
| :--- | :---: |
| LED symbol correct and marked L1 | 1 |
| circuit connected to output pin on one side | 1 |
| resistor in series with LED | 1 |
| circuit ends at GND (either GND) | 1 |
|  | $\mathbf{4}$ |

(c) Use the diagram below to draw a voltage regulator circuit to take a 9 V battery and provide the microcontroller the 5 V supply it requires.


| Description | Marks |
| :--- | :---: |
| 9 V DC symbol used | 1 |
| 9 V supply connected correctly | 1 |
| capacitor 1 inserted and correct value | 1 |
| capacitor 2 inserted and correct value | 1 |
| 7805 used and marked correctly | 1 |
| 7805 IC connected correctly | 1 |
| correct pins connected to on microcontroller | 1 |
|  | $\mathbf{7}$ |

Question 45 (continued)
(d) The controller will use an output for a DPDT relay Y 1 , which will be used as a H bridge that will drive a motor M1 from a separate 10 A 24 V DC source. It will also use a SPDT relay Y2 triggered by an output to turn the motor power off and on. Draw this configuration, using the diagram below.


| Description | Marks |  |  |
| :--- | :---: | :---: | :---: |
| DPDT relay component used and marked as Y1 | 1 |  |  |
| output pin used for Y1 coil | 1 |  |  |
| one side of Y1 coil connected to ground | 1 |  |  |
| motor marked as M1 | 1 |  |  |
| motor Connected correctly | 1 |  |  |
| correct supply symbol used | 1 |  |  |
| supply marked 24 V 10 A | 1 |  |  |
| supply connected correctly to DPDT | 1 |  |  |
| SPDT relay used and marked as Y2 | 1 |  |  |
| output pin used for Y2 coil | 1 |  |  |
| one side of Y2 coil connected to ground | 1 |  |  |
| Y2 switch breaks power to M1 | 1 |  |  |
| Total |  |  | $\mathbf{1 2}$ |
| errors carried forward full marks (misidentified pins only) |  |  |  |

## Question 46

(a) When the motor is rotating at 300 rpm , how fast is the winch rotating?

| Description | Marks |  |
| :--- | :---: | :---: |
| $\mathrm{v}_{\mathrm{w}}=300 / 35$ |  | 1 |
| $\mathrm{v}_{\mathrm{w}}=8.57 \mathrm{rpm}$ | Total | $\mathbf{1}$ |

(b) If the motor is rotating at 300 rpm , how fast is the weight rising? If you did not get an answer for part (a), use 9 rpm .

| Description | Marks |
| :--- | :---: |
| $\mathrm{v}_{1}=\mathrm{v}_{\mathrm{w}} \times 2 \times \pi \times \mathrm{r} / 60$ <br> derive equation | 1 |
| Use $\mathrm{v}_{\mathrm{w}}=8.57 \mathrm{rpm}$ from a <br> $\mathrm{r}=\mathrm{d} / 2=0.1 \mathrm{~m}$ | 1 |
| $\mathrm{v}_{1}=5.38 \mathrm{~m} / \mathrm{min}^{2}$ or <br>  <br> $=0.0897 \mathrm{~ms}^{-1}\left(0.0942 \mathrm{~ms}^{-1}\right)$ | 1 |
| Accept other methods of deriving correct answer |  |

(c) At what rate does the motor need to spin for the weight to rise at $0.10 \mathrm{~m} \mathrm{~s}^{-1}$ ? (3 marks)

| Description | Marks |
| :--- | :---: |
| $\mathrm{v}_{\mathrm{L}}=0.1 \mathrm{~m} / \mathrm{s}$ |  |
| $\mathrm{r}=0.1 \mathrm{~m}$ |  |
| $\mathrm{~V}_{\mathrm{L}}=\mathrm{v}_{\mathrm{w}} \times 2 \times \pi \times \mathrm{r} / 60$ | $1-2$ |
| $\mathrm{~V}_{\mathrm{w}}=9.55 \mathrm{rpm}$ |  |
| $\mathrm{V}_{\mathrm{m}}=\mathrm{v}_{\mathrm{w}} \times 35$ |  |
| $\mathrm{~V}_{\mathrm{m}}=334 \mathrm{rpm}$ | 1 |
| Accept other methods of deriving correct answer |  |

(d) For what period of time does the motor need to spin at 300 rpm for the weight to have risen 1.20 m ? If you did not get an answer for part (b), use $95 \mathrm{~mm} \mathrm{~s}^{-1}$.

| Description | Marks |
| :---: | :---: |
| $1.20 / 0.0897$ | $1-2$ |
| $\mathrm{t}=13.4 \mathrm{~s}(12.6 \mathrm{~s})$ | $\mathbf{1}$ |
|  | Total |

(e) If the velocity ratio is 1.01 and the distance moved by the load is 1.30 m , calculate the distance moved by the effort.

| Description | Marks |  |
| :--- | :---: | :---: |
| $d_{e}=1.01 \times 1.3 \mathrm{~m}$ <br> $d_{e}=1.31 \mathrm{~m}$ | 1 |  |
|  | Total | $\mathbf{1}$ |

Question 46 (continued)
(f) If the effective diameter of the output shaft of the gearbox is 20 mm does the winch or the gearbox have greater mechanical advantage in this system and why?

| Description | Marks |
| :--- | :---: |
| gearbox | 1 |
| winch advantage is 20:200 or 1:10 | 1 |
| gearbox advantage is $35: 1$ | 1 |
|  | $\mathbf{3}$ |

## ACKNOWLEDGEMENTS

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