



# ENGINEERING STUDIES ATAR COURSE DATA BOOK 2017

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This document is valid for teaching and examining until 31 December 2017.

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## SI units

Quantity	SI unit		
Quantity	Name	Symbol	
Length	metre	m	
Mass	kilogram	kg	
Time	second	S	
Energy, work, quantity of heat	joule	J	
Power	watt	W	
Celsius temperature	degree Celsius	С°	
Area	square metre	m²	
Volume	cubic metre	m <sup>3</sup>	
Speed, velocity	metre per second	m s⁻¹	
Mass density	kilogram per cubic metre	kg m⁻³	

# Standard prefixes

Factor	Prefix	Symbol	Factor	Prefix	Symbol
10 <sup>12</sup>	tera	Т	10 <sup>-3</sup>	milli	m
10 <sup>9</sup>	giga	G	10 <sup>-6</sup>	micro	μ
10 <sup>6</sup>	mega	М	10 <sup>-9</sup>	nano	n
10 <sup>3</sup>	kilo	k	10 <sup>-12</sup>	pico	р

#### **Common constant**

Item	Symbol	Value
Ratio of the circumference of a circle to its diameter	π	3.14159

#### ENGINEERING STUDIES CORE CONTENT

#### **General formulae**

Parameter	Formula	Terms
Side lengths of a right triangular plane figure	$h^2 = o^2 + a^2$	<i>h</i> is the hypotenuse <i>o</i> is the opposite side <i>a</i> is the adjacent side
Angular relationships of a right triangular figure	$\cos \theta = \frac{a}{h}$ $\sin \theta = \frac{o}{h}$ $\tan \theta = \frac{o}{a}$	$\theta$ is the angle <i>h</i> is the hypotenuse <i>o</i> is the opposite side <i>a</i> is the adjacent side
Perimeter of a circle [p]	$p = \pi d$	<i>d</i> is the diameter
Area of a circle [A]	$A = \pi r^2$	r is the radius
Surface area of open ended cylinder [ <i>A</i> ]	$A = \pi dh$	<i>d</i> is the diameter <i>h</i> is the height
Volume of a cylinder [V]	$V = \pi r^2 h$	<i>r</i> is the radius <i>h</i> is the height
Surface area of a sphere [ <i>A</i> ]	$A = 4\pi r^2$	r is the radius
Volume of a sphere [V]	$V = \frac{4}{3}\pi r^3$	r is the radius
Density $[\rho]$ of a material	$\rho = \frac{m}{V}$	<i>m</i> is mass <i>V</i> is volume
Energy [E]	E = Pt	<i>t</i> is the time taken <i>P</i> is the power
Efficiency [η] %	$\eta\% = \frac{Output}{Input} \times 100$	$\eta$ is the efficiency (%)

## Selected material properties

Material	Density kg m <sup>-3</sup>	Elastic (Young's) modulus kN mm <sup>-2</sup>	Ultimate tensile * strength N mm <sup>-2</sup>	Yield stress N mm <sup>-2</sup>	Electrical conductivity Ω <sup>-1</sup> m <sup>-1</sup> × 10 <sup>6</sup>	Thermal conductivity W m <sup>-1</sup> K <sup>-1</sup>
Structural steel	7850	200	470	250	13.0	46
Stainless steel	7600	200	860	502	1.35	16
Cast iron	7200	120	180		10.3	80
Wrought iron	7750	200			10.3	80
	1				1	
Aluminium	2710	70	150	95	37.7	237
Brass	8740	90	190	50	16.7	109
Copper	8930	112	210	70	59.5	401
Zinc	7130	108	200	13.8	16.8	116
Solder (60% lead, 40% tin)	9280	23.7	37	-	7.28	43.6
Concrete	2400	30	40 (compressive)			0.8
Concrete (steel reinforced)						0.8
Timber (parallel to grain)		12	105			0.16
Polypropylene	1240	4	19.7 – 80	50		0.13
Polycarbonate	1200	2.3	70			0.19
ABS plastics		2.3	40	48.3		2.34
Nylon	1160	2-4	75	45		
Acrylic	1190	3.2	70	73.7		0.19
	1					
Glass	2500	69		3600		1.05
Diamond	3520	1000		50 000		2320
Gold	19 320	82	220	40	44.6	318
Ice	931	9.17.5@-5°C		85		2.25@-5°C
Pure water	1000					
Sea water	1022					
Petrol	740					0.15
Crude oil	800					0.15

\* Unless noted as compressive strength.

#### ENGINEERING STUDIES SPECIALIST FIELD MECHANICAL

#### DATA BOOK

# Basic formulae (Mechanical) 1

Parameter	Formula	Terms
Mechanical Advantage	Fload	$F_{load}$ is the output force
[ <i>MA</i> ]	$MA = \frac{1}{5}$	$F_{effort}$ is the input force
	F effort	
Velocity Ratio [VR]	$_{\rm LZD} = d_{\it effort}$	$d_{effort}$ is the distance moved by the
	$V R = \frac{d_{load}}{d}$	effort
		<i>d</i> <sub>load</sub> is the distance moved by the load
Velocity ratios in drive	$F_1$ $F_2$ $F_3$	$F_{I,2 \text{ and } 3}$ are the followers
trains	$VR = \frac{1}{D_1} \frac{1}{D_2} \frac{1}{D_2}$	$D_{1,2 \text{ and } 3}$ are the drivers
(for gear or pulley train )	$D_1 D_2 D_3$	(measured via number of teeth on
		gears or by pulley diameters)
Torque [τ]	au = Fr	F is the force
	V 11	r is the radius
Moment of a force [M]	M = Fd	<i>F</i> is the force
		<i>d</i> is the perpendicular distance
Stress[ $\sigma$ ] or Pressure [ $p$ ]	$-\langle r \rangle$ F	<i>F</i> is the force
	$\sigma(p) = \frac{1}{A}$	<i>A</i> is the area
Strain [ɛ]	$\Delta L$	$\Delta L$ is the change in length
	$\mathcal{E} = \frac{\Delta E}{L}$	L is the original length
	L	
Young's (Elastic) modulus	$_{F}-\sigma$	$\sigma$ is the stress
	$E = \frac{1}{\varepsilon}$	$\varepsilon$ is the strain
Young's (Elastic) modulus		<i>F</i> is the force
[E] expanded formula	F FL	A is the area
	$E = \frac{1}{4 \Lambda I}$	$\Delta L$ is the change in length
		L is the original length
Factor of Safety [FS]	<i>G</i>	$\sigma_{UTS}$ is the ultimate tensile stress
	$FS = - \frac{O_{UTS}}{-}$	$\sigma_{\rm eff}$ is the safe working stress
	<i>O</i> <sub>safeworking</sub>	
Acceleration [a]	a - v - u	v is the final velocity
	$a = \frac{t}{t}$	<i>u</i> is the initial velocity
		t is the time
Velocity [v]		<i>u</i> is the initial velocity
	$v^2 = u^2 + 2as$	<i>a</i> is the acceleration
		s is the distance
Distance [s]	$s = ut + \frac{1}{2}at^{2}$	<i>u</i> is the initial velocity
	/ 2	<i>t</i> is the time
		<i>a</i> is the acceleration
Force [F]	F = ma	<i>m</i> is the mass
		<i>a</i> is the acceleration
Equilibrium conditions	$\sum M = 0$	$\varSigma$ is the 'sum of'
		M are the moments
	$\sum F_{ij} = 0$	$F_y$ are the vertical force components
	y S	$F_x$ are the horizontal force
	$\sum F_x = 0$	components
Equilibrium conditions	$\Sigma CWM = \Sigma ACWM$	$\varSigma$ is the 'sum of'
(expanded)	$\Sigma E(up) = \Sigma E(down)$	CWM are clockwise moments
	$\sum (up) = \sum (uown)$	ACWM are anticlockwise moments
	$\Sigma F(left) = \Sigma F(right)$	

## Basic formulae (Mechanical) 2

Parameter	Formula	Terms
Work [W]	W = Fs	<i>F</i> is the force
		s is the distance moved
Power [P]	p Fs p	F is the force
	$P = \frac{1}{t} = Fv$	s is the distance
		<i>t</i> is the time taken
		v is the average velocity
Energy [E]	E = Pt	<i>t</i> is the time taken
		<i>P</i> is the power
Potential energy	$E_{n} = mgh$	<i>m</i> is the mass
$[E_p]$	p C	g is the acceleration due to gravity
		<i>h</i> is the height
Kinetic energy $[E_k]$	$E_{\mu} = \frac{1}{2}mv^2$	<i>m</i> is the mass
	~ / 2	v is the velocity
Potential and kinetic energy conversion	$\Delta E_p = \Delta E_k$	$\Delta$ is the 'change in'
Efficiency [ $\eta$ ] %	$\eta\% = \frac{Work \ done \ in \ moving \ load}{W} \times 100$	Work done in moving load is the output
	<i>Work done by the effort</i>	Work done by the effort is the input
Compound gear or	input RPM	VR is the velocity ratio
pulley system [RPM]	$output RPM = \frac{VR}{VR}$	<i>RPM</i> is the revolutions per minute
Linear velocity of a	$(RPM)(2\pi r)$ s	<i>r</i> is the radius of the gear or pulley
gear or pulley	$v = \frac{1}{60} = \frac{1}{t}$	s is the distance travelled
	00 1	<i>t</i> is the time taken
Distance around a	$s = 2\pi r$	r is the radius of the drum
winch drum [s]		

## **Selected SI units**

			SI unit	Fypression		
Derived quantity	ved quantity Name		Expression in terms of other SI units	Expression in terms of SI base units		
Force	newton	Ν	-	m kg s⁻²		
Pressure, stress	pascal	Pa	N m <sup>-2</sup>	m⁻¹ kg s⁻²		
Energy, work, quantity of heat	joule	J	N m	m² kg s⁻²		
Power, radiant flux	watt	W	_	m² kg s⁻³		

#### **Common constants**

Item	Symbol	Value
Acceleration due to gravity	g	9.80 m s <sup>−2</sup>

#### Second moment of area

Shape	Dimensions	Second moment of area about centroidal axis
Rectangle solid section (vertical)	$x \xrightarrow{h}$	$I_{xx} = \frac{bh^3}{12}$
Circular solid section		$I_{xx} = \frac{\pi D^4}{64}$
Circular tube section		$I_{xx} = \frac{\pi (D_o^4 - D_i^4)}{64}$ D_o = cylinder outside diameter D_i = cylinder inside diameter

#### Simple beams

Beam configuration	Maximum bending moment	Maximum deflection (y)
A B	$BM_{max} = FL$ at $A$ Here $F$ is the single vertical point load	$y = \frac{FL^3}{3EI_{xx}}  at B$ Here <i>F</i> is the single vertical point load
$F_{UDL} = \omega L$	$BM_{\text{max}} = \frac{F_{UDL}L}{2}  at A$ Here $F_{UDL}$ = $\omega L$ which is the load per unit length ( $\omega$ ) times the length of the beam ( $L$ )	$y = \frac{F_{UDL}L^3}{8EI_{xx}}  at B$ Here $F_{UDL} = \omega L$ which is the load per unit length ( $\omega$ ) times the length of the beam (L)
	$BM_{\text{max}} = \frac{FL}{4}  at C$ Here <i>F</i> is the single vertical point load	$y = \frac{FL^3}{48EI_{xx}}  at C$ Here <i>F</i> is the single vertical point load
$F_{UDL} = \omega L$	$BM_{max} = \frac{F_{UDL}L}{8}  at C$ Here $F_{UDL} = \omega L$ which is the load per unit length ( $\omega$ ) times the length of the beam (L)	$Y = \frac{5F_{UDL}L^3}{384EI_{xx}}  at C$ Here $F_{UDL} = \omega L$ which is the load per unit length ( $\omega$ ) times the length of the beam (L)

### Terms:

- *L* Length of beam between supports
- $\omega$  A uniformly distributed load per unit length
- $F_{\textit{UDL}}$  The product of the UDL's applied load/unit length ( $\omega$ ) and the length of the beam (L)
  - *F* An applied vertical point load
  - *E* The elastic (Young's) modulus of the material of the beam
  - $I_{xx}$  The second moment of area of the beam section
  - *A* The left-hand end of the beam
  - *B* The right-hand end of the beam
  - C The mid-point of the beam

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## ENGINEERING STUDIES SPECIALIST FIELD MECHATRONICS

#### Selected SI units

Quantity	Unit	Abbreviation	Symbol	Expression in terms of other SI units
Voltage	volt	V	V	W A <sup>-1</sup>
Current	ampere	A	Ι	W V <sup>-1</sup>
Resistance	ohm	Ω	R	V A <sup>-1</sup>
Charge	coulomb	С	Q	As
Capacitance	farad	F	С	A s V <sup>-1</sup>
Power	watt	W	Р	J s⁻¹
Frequency	hertz	Hz	f	S <sup>-1</sup>

#### Prefixes

Prefix	Abbreviation		Multiplier
Tera	Т	10 <sup>12</sup>	= 1 000 000 000 000
Giga	G	10 <sup>9</sup>	= 1 000 000 000
Mega	М	10 <sup>6</sup>	= 1000 000
Kilo	k	10 <sup>3</sup>	= 1000
		10 <sup>0</sup>	= 1
Milli	m	10 <sup>-3</sup>	= 0.001
Micro	μ	10 <sup>-6</sup>	= 0.000 001
Nano	n	10 <sup>-9</sup>	= 0.000 000 001
Pico	р	10 <sup>-12</sup>	= 0.000 000 000 001

Standard symbols



#### ENGINEERING STUDIES SPECIALIST FIELD MECHATRONICS

#### **Resistor colour codes**

Band colour	1st band	2nd band	Multiplier
Black		0	1
Brown	1	1	10
Red	2	2	100
Orange	3	3	1000
Yellow	4	4	10 000
Green	5	5	100 000
Blue	6	6	1 000 000
Violet	7	7	
Grey	8	8	
White	9	9	

Tolerance band			
Brown	± 1%		
Red	± 2%		
Gold	± 5%		
Silver	± 10%		

E12 Preferred values: 10, 12, 15, 18, 22, 27, 33, 39, 47, 56, 68, 82

Example: 4 band colour code



## Electrical formula wheel



# Basic formulae (Mechatronics) 1

Parameter	Formula	Terms
Ohm's law	V = IR	<i>V</i> is the voltage
		<i>I</i> is the current
		<i>R</i> is the resistance
Power law	$\sim V^2$	<i>P</i> is the power
	$P = VI = I^2 R = \frac{1}{R}$	<i>I</i> is the current
	I. I	V is the voltage
		<i>R</i> is the resistance
Electrical energy $[E_e]$	$E_e = VIt$	<i>V</i> is the voltage
		<i>I</i> is the current
		<i>t</i> is the time
Resistors in series	$R_t = R_1 + R_2 + \dots$	$R_t$ is the total resistance
		$R_1, R_2, \ldots$ are the individual resistances
Resistors in parallel	1 1 1	$R_t$ is the total resistance
	$\overline{R_t} = \overline{R_1} + \overline{R_2} + \cdots$	$R_1, R_2, \ldots$ are the individual resistances
Kirchhoff's first law	$\sum I = 0$	The sum of currents flowing toward that point
		from that point
Kirchhoff's second law	$\Sigma \Lambda V = 0$	The directed sum of the electrical potential
		differences around a closed loop in a circuit
Conceitore in norellal		must be zero
	$C = C_1 + C_2 + \cdots$	C is the total capacitance
Capacitora in corico	1 1 1	$C_1, C_2, \dots$ are the individual capacitances
Capacitors in series	$\frac{1}{2} = \frac{1}{2} + \frac{1}{2} + \cdots$	C is the total capacitance
	$C  C_1  C_2$	$C_1, C_2, \dots$ are the individual capacitances
Voltage dividers	$V_{cc} = V_1 + V_2$	$V_{cc}$ is the total voltage across the resistor pair
	R <sub>1</sub>	$V_I$ is the voltage across resistor R <sub>1</sub>
	$V_1 = V_{cc} \frac{1}{R_1 + R_2}$	$V_2$ is the voltage across resistor $R_2$
	$R_2$	
	$V_2 = V_{cc} \frac{1}{R_1 + R_2}$	
LED in series with a		$V_{cc}$ is the total applied voltage
resistor	$R - \frac{\left(V_{cc} - V_{LED}\right)}{\left(V_{cc} - V_{LED}\right)}$	$V_{LED}$ is the voltage across the LED
	$R = \frac{I_{LED}}{I_{LED}}$	$I_{LED}$ is the current through the LED
		<i>R</i> is the series resistor
Transistor current gain	$I_{h} = I_{C}$	$I_C$ is the collector current
	$n_{FE} = \frac{1}{I_{R}}$	$I_B$ is the base current
1	D	

### ENGINEERING STUDIES SPECIALIST FIELD MECHATRONICS

#### DATA BOOK

## Basic formulae (Mechatronics) 2

Parameter	Formula	Terms
Mechanical advantage ( <i>MA</i> )	$MA = \frac{\text{load}}{\text{effort}}$	
Velocity ratio ( <i>VR</i> )	$VR = rac{ ext{distance moved by effort}}{ ext{distance moved by load}}$	
Pulley belt ratio	$VR = \frac{\emptyset \text{ follower pulley}}{\emptyset \text{ driver pulley}}$	
Chain and sprocket ratio	$VR = rac{n^{\circ}  ext{ teeth follower gear}}{n^{\circ}  ext{ teeth driver gear}}$	
Gear ratio	$VR = rac{n^{\circ}  ext{ teeth follower gear}}{n^{\circ}  ext{ teeth driver gear}}$	
Compound gear ratio	$VR_T = VR_1 \times VR_2 \times \dots$	$VR_T$ is the total velocity ratio $VR_1$ , $VR_2$ , are the individual velocity ratios
Worm and worm wheel ratio	$VR = \frac{n^{\circ} \text{ teeth worm wheel}}{1}$	
Rack and pinion	$distance = \frac{n^{\circ} \text{ teeth pinion } \times n^{\circ} \text{ revolutions}}{n^{\circ} \text{ teeth per metre rack}}$	
Speed, velocity	$velocity = \frac{distance}{time} = \frac{(rpm)(2\pi r)}{60}$	
	$output rpm = \frac{input rpm}{VR}$	<i>VR</i> is the velocity ratio <i>rpm</i> is the revolutions per minute

#### SI units

Quantity	SI unit		
Quantity	Name	Symbol	
Length (distance)	metre	m	
Time	second	S	
Speed, velocity	metre per second	m s⁻¹	

#### Diodes

Diode model	Formula	Terms/diagrams
On	$V_D = V_{D,on} \text{ (or } V_F)$ Check: $I_D > 0$	
Off	$I_D = 0 \text{ A}$ Check: $V_D < V_{D,on} \text{ (or } V_F \text{)}$	anode (a) • • cathode (k) + $V_D$ -

## Transistors

Transistor model (NPN BJT)	Formula	Terms/diagrams
Cut-off	$I_B = I_C = 0 \text{ A}$ Check: $V_{BE} < 0.7 \text{ V}$	
Saturation	$V_{BE} = 0.7 V$ $V_{CE} = 0 V$ <b>Check:</b> $I_B > 0 A$ $\frac{I_C}{I_B} < \beta \text{ (or } h_{FE})$	Base $I_B$ $V_{BE}$ $I_E$ $I_C$ $V_{CE}$ $I_E$
Forward-active	$V_{BE} = 0.7 V$ $I_C = \beta \times I_B$ <b>Check:</b> $I_B > 0 A$ $V_{CE} > 0 V$	Emitter
Transistor current gain	Gain or $\beta$ or $h_{FE} = \frac{I_C}{I_B}$	$I_{C}$ is the collector current $I_{B}$ is the base current

## Logic symbols with truth tables and Boolean expressions



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#### ACKNOWLEDGEMENTS

Page 12Electrical formula wheel. Retrieved January, 2010, from<br/>www.sengpielaudio.com/calculatorohm.htm#top.

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